



Sous la co-tutelle de :

CNRS
ÉCOLE DES PONTS PARISTECH
UNIVERSITÉ GUSTAVE EIFFEL

2024-11-14

Formalization of real query languages and application to theory



Claire David



Nadime Francis



Victor Marsault

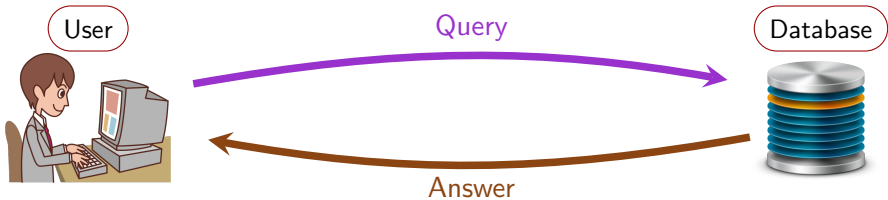


Antoine Meyer

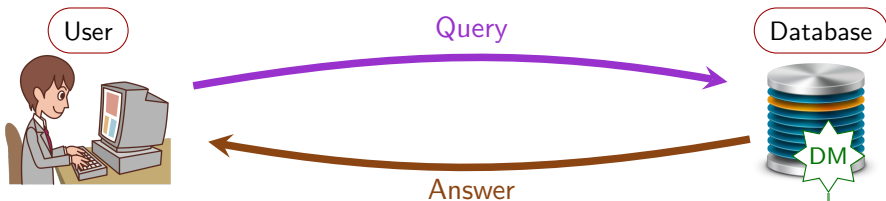


Liat Peterfreund

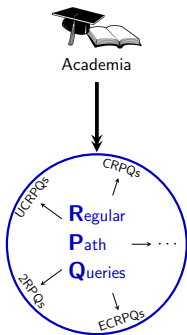
and many other coauthors from academia and industry



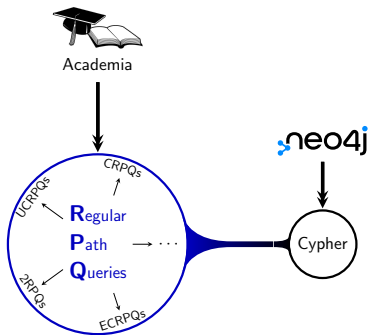
- Query language
 - *"What can the user write?"*



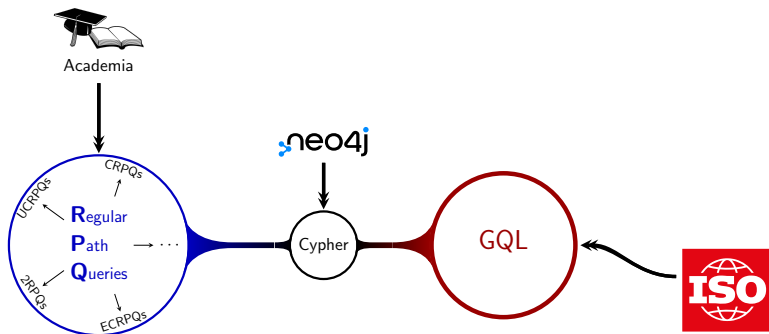
- Semantics of query
 - *"What data is extracted?"*
- DM = Data model
 - *"How the data is structured"*



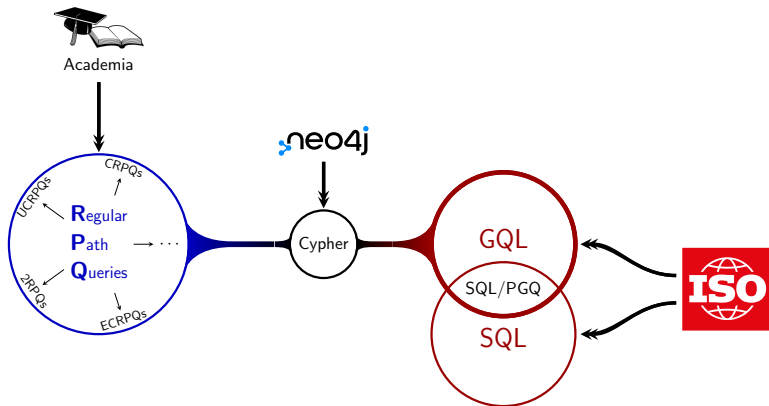
- RPQs (1990's) pattern matching with regular expressions



- **RPQs (1990's)** pattern matching with regular expressions
- **Cypher (2011)** query language for a new data model (property graphs)



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- GQL (2024) standard query language for property graphs



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- GQL (2024) standard query language for property graphs
- SQL/PGQ (2023) support for querying property graphs from SQL

1 Formalize

- Collaboration with private actors
- Access to database engine and/or documentation
- Produce formal semantics of query languages

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2 Observe what is done in practice

- “Strange” decisions
- Discrepancies with theoretical models
- Goals and needs

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3 Apply to theory

- Propose theoretical models closer to reality
- Adapt algorithms
- Propose features in line with practice

2019

Formalization of
Cypher (Neo4j)

[FG⁺18; GG⁺19]



2019

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Formalization of
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[DF⁺22; FG⁺23a; FG⁺23b; ISO24]



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RPQ semantics used in
practice all have issues

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A new RPQ
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[DFM23; DFMS??]



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GQL
v2.0

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Framework for
RPQ semantics

[Work in progress]



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Schemas for
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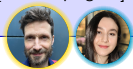
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Formalization of **GQL** (Neo4j et ISO)

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Schemas for GQL [AB⁺23]



Data model in GQL is
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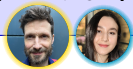
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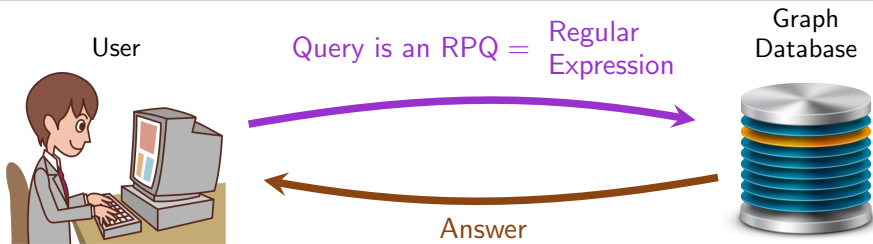
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Efficient algorithm for
shortest semantics
in GQL model [DFM24]



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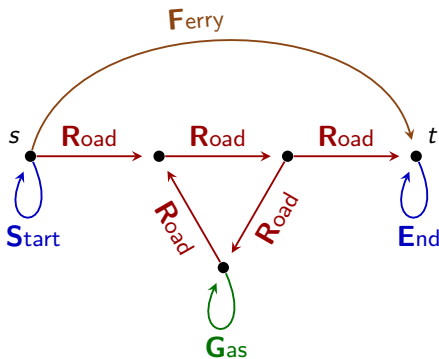
**Focus on [DFM23]:
Run-based semantics for RPQs**



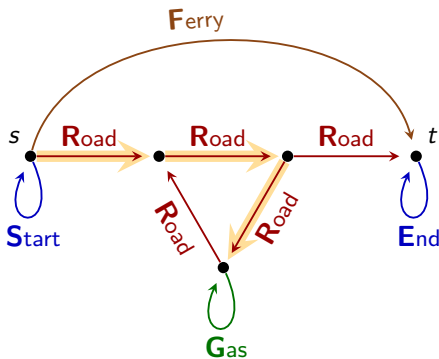
Our database is a labeled graph



- Finite label alphabet:
 $\Sigma = \{\text{S}, \text{R}, \text{F}, \text{G}, \text{E}\}$
- Vertices
- Edges labelled over Σ



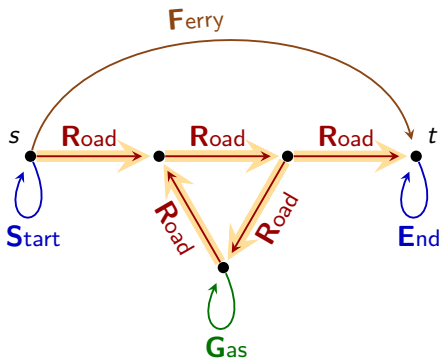
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Terminology: Walk

- Consistent sequence of edges
- Repetitions are allowed

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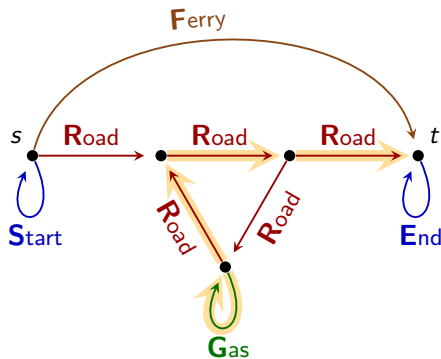
Terminology: Walk

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$Q ::= \mathbf{A}$ Atoms
 QQ Concatenation
 $Q + Q$ Disjunction
 Q^* Kleene star
 where $\mathbf{A}$ is a label in the graph.

Ex: $\mathbf{GR}^*$

*"One **G** then any number of **R**"*



Definition

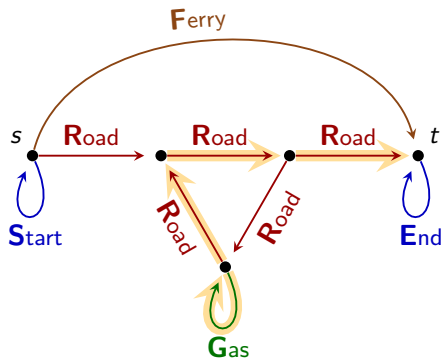
A walk matches Q
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⚠ Infinitely many matches ⚠

How to ensure finiteness ?

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Endpoint semantics

- Main semantics in theory
- Return endpoints of matches

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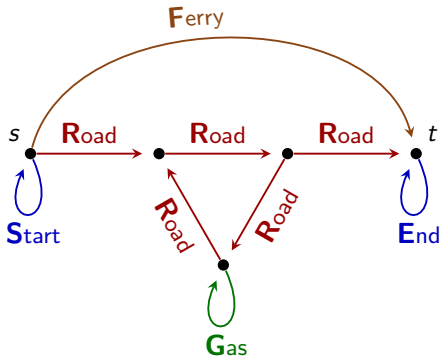
Binding-trail semantics

- Our proposal
- Edges may be repeated when using different atoms

Finding a way from s to t



$$Q_1 = \mathbf{S} (\mathbf{R} + \mathbf{F})^* \mathbf{E}$$

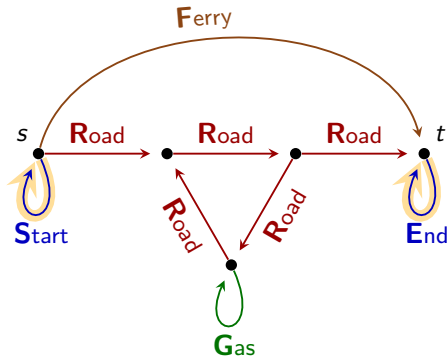


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Which walks match Q_1 ?



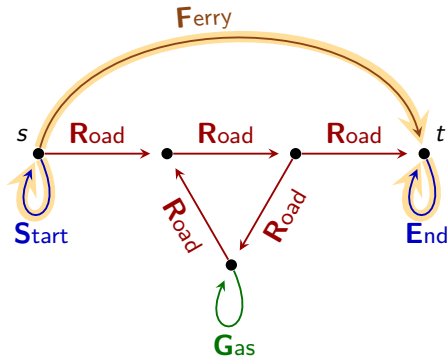
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Which walks match Q_1 ?

- The ferry



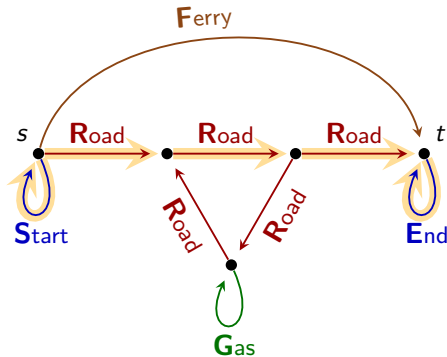
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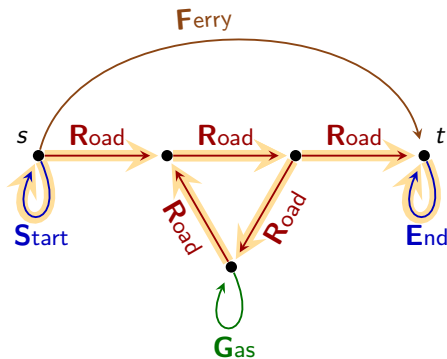
- The ferry
- The straight road



$$Q_1 = \mathbf{S} (\mathbf{R} + \mathbf{F})^* \mathbf{E}$$

Which walks match Q_1 ?

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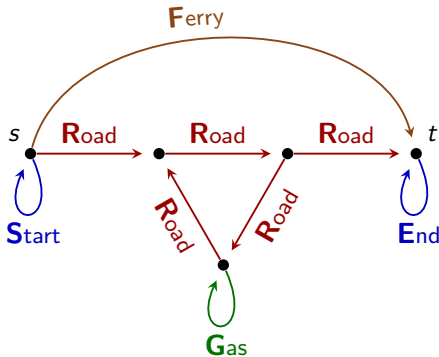
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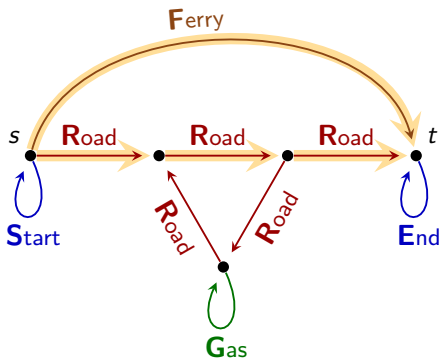
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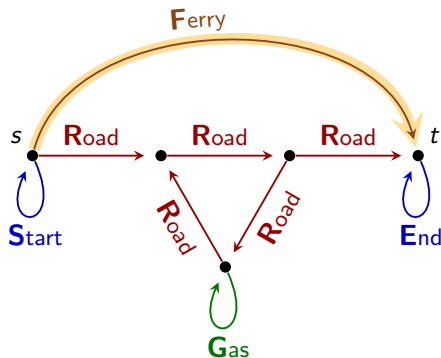
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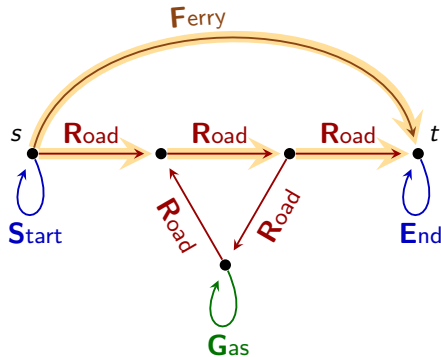
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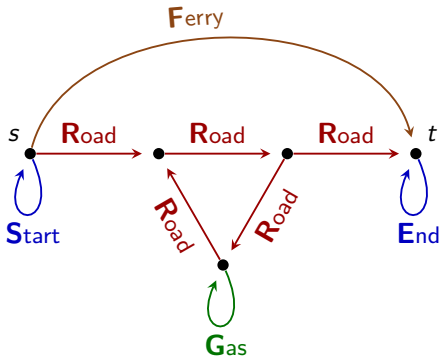
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Binding-trail returns the ferry and the straight road

$$Q_2 = \text{S } (\text{R} + \text{F})^* \text{ G } (\text{R} + \text{F})^* \text{ E}$$

Which walks match Q_2 ?

- Walks with ≥ 1 circuit laps



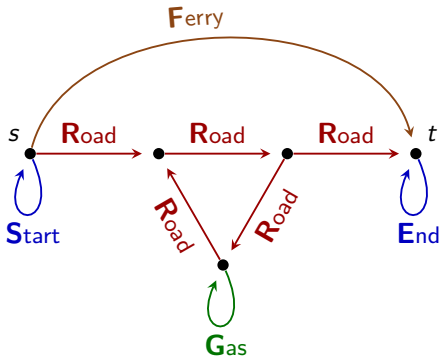
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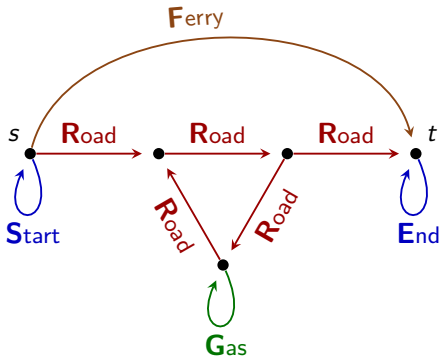
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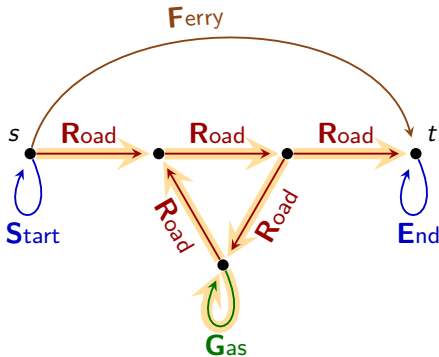
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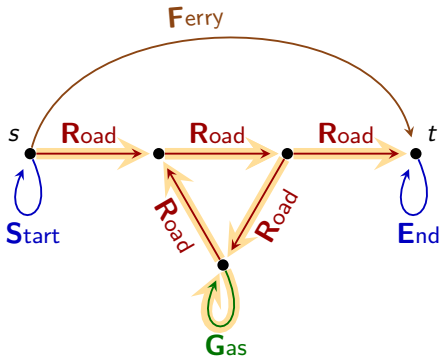
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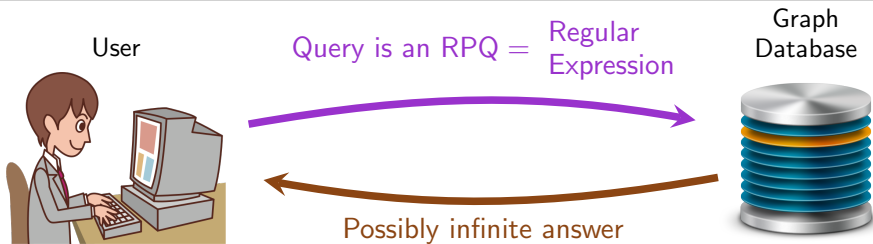
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Binding-trail returns the walk with 1 circuit lap.



Question: How to ensure finiteness?

In theory

Endpoint semantics

- Little information is returned

Our proposal

Binding-trail semantics

- A good compromise?

In practice

Trail semantics

- Untractable
- Shortest sem.**
- Arbitrary

Ongoing/Future work

2019

2022

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[FG⁺18; GG⁺19]

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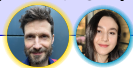
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[Work in progress]



GraphQL
v2.0

Formalization of **GQL** (Neo4j et ISO)

[DF⁺22; FG⁺23a; FG⁺23b; ISO24]

Schemas for
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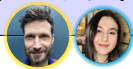
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Rel manipulates
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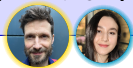
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[Work in progress]

Rel manipulates
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queries

[Work in progress]

GQL
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- [AB⁺23] R. Angles, A. Bonifati, S. Dumbrava, G. Fletcher, A. Green, J. Hidders, B. Li, L. Libkin, V. Marsault, W. Martens, F. Murlak, S. Plantikow, O. Savković, M. Schmidt, J. Sequeda, S. Staworko, D. Tomaszuk, H. Voigt, D. Vrgoč, M. Wu, and D. Živković. “PG-Schema: Schemas for Property Graphs”. In: *Proceedings of the ACM on Management of Data (SIGMOD)*. Vol. 1. 2. Industrial Track. ACM, June 2023.
- [DFM23] C. David, N. Francis, and V. Marsault. “Run-Based Semantics for RPQs”. In: *Principles of Knowledge Representation and Reasoning (KR’23)*. Aug. 2023, pp. 178–187.
- [DFM24] C. David, N. Francis, and V. Marsault. “Distinct Shortest Walk Enumeration for RPQs”. In: *PODS*. Vol. 2. 2. ACM, 2024. URL: <https://doi.org/10.1145/3651601>.
- [DF⁺22] A. Deutsch, N. Francis, A. Green, K. Hare, B. Li, L. Libkin, T. Lindaaker, V. Marsault, W. Martens, J. Michels, F. Murlak, S. Plantikow, P. Selmer, H. Voigt, O. van Rest, D. Vrgoč, M. Wu, and F. Zemke. “Graph Pattern Matching in GQL and SQL/PGQ”. In: *SIGMOD’22*. 2022. URL: <https://doi.org/10.1145/3514221.3526057>.

- [FG⁺23a] N. Francis, A. Gheerbrant, P. Guagliardo, L. Libkin, V. Marsault, W. Martens, F. Murlak, L. Peterfreund, A. Rogova, and D. Vrgoč. “A Researcher’s Digest of GQL”. In: *ICDT*. Invited talk. 2023. URL: <https://doi.org/10.4230/LIPIcs.ICDT.2023.1>.
- [FG⁺23b] N. Francis, A. Gheerbrant, P. Guagliardo, L. Libkin, V. Marsault, W. Martens, F. Murlak, L. Peterfreund, A. Rogova, and D. Vrgoč. “GPC: A Pattern Calculus for Property Graphs”. In: *PODS’23*. 2023. URL: <https://doi.org/10.1145/3584372.3588662>.
- [FG⁺18] N. Francis, A. Green, P. Guagliardo, L. Libkin, T. Lindaaker, V. Marsault, S. Plantikow, M. Rydberg, P. Selmer, and A. Taylor. “Cypher: An Evolving Query Language for Property Graphs”. In: *SIGMOD’18*. ACM, 2018. URL: <http://dx.doi.org/10.1145/3183713.3190657>.
- [ISO24] *GQL*. Standard ISO/IEC CD 39075. International Organization for Standardization (ISO), 2024. URL: <https://www.iso.org/standard/76120.html>.

- [GG⁺19] A. Green, P. Guagliardo, L. Libkin, T. Lindaaker, V. Marsault, S. Plantikow, M. Schuster, P. Selmer, and H. Voigt. “Updating Graph Databases with Cypher”. In: *VLDB*. 2019. URL: <https://doi.org/10.14778/3352063.3352139>.

Q_1 in Cypher

```
MATCH ({id:"Paris"}) -[:Road|Ferry*]-> ({id:"Lyon"})
```

Q_2 in GQL

```
MATCH(s WHERE s.id="Paris")  
  -[IS Road|Ferry]->* (m WHERE m.hasGas=true)  
  -[IS Road|Ferry]->* (t WHERE t.id="Lyon")
```